



**MAXIMAL EFFICIENCIES IN -ALLOY JUNCTION SOLAR CELLS  
AT 300 K, ACCORDING TO HIGHEST HOT RESERVOIR  
TEMPERATURES, OBTAINED FROM CARNOT-EFFICIENCY  
THEOREM. (VI)**

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**ABSTRACT**

In  $n^+(p^+) - p(n)$  [ $X(x) \equiv \text{GaP}_{1-x}\text{As}_x$ ]-alloy junction solar cells at  $T=300$  K,  $0 \leq x \leq 1$ , by basing on the same physical model and the same treatment method, as those used in our recent works<sup>[1,2]</sup>, we will also investigate the maximal efficiencies,  $\eta_{I\text{max.}(II\text{max.})}$ , obtained at the open circuit voltage  $V_{oc}(=V_{ocI(ocII)})$ , according to highest hot reservoir temperatures,  $T_H(K)$ , obtained from the Carnot efficiency theorem, which was demonstrated by the use of the entropy law. In this word, some concluding remarks are given in the following. **(1)** In the heavily doped emitter region, the effective density of electrons (holes),  $N^*$ , given in parabolic conduction (valence) bands, expressed as functions of the total dense impurity density,  $N$ , donor (acceptor)-radius,  $r_{d(a)}$ , and  $x$ -concentration, is defined in Eq. (9d), as:

$N^*(N, r_{d(a)}, x) \equiv N - N_{CDn(NDp)}(r_{d(a)}, x)$ , where  $N_{CDn(NDp)}$  is the Mott critical density in the metal-insulator transition, determined in Eq. (9a). Then, we have showed that (i) the origin of such the Mott's criterium, Eq. (9a), is exactly obtained from the reduced effective Wigner-Seitz radius  $r_{sn(sp)}$ , characteristic of interactions, as that given in Equations (9b, 9c), and further (ii)  $N_{CDn(CDp)}$  is just the density of electrons (holes) localized in the exponential conduction (valence)-band tail (EBT), as that demonstrated in<sup>[1]</sup> **(2)** In Table 3n, for

$n^+ - p$  X(x) –alloy junction solar cell and for  $r_{Sn(Cd)}$ -radius, one obtains with increasing  $x=(0, 0.5, 1)$ :  $\eta_{I_{max.}(\lambda)} = 32.83\%$ , 31.96%, 31.15%, according to  $T_H(\lambda) = 446.6 \text{ K}, 440.9 \text{ K}, 435.7 \text{ K}$ , at  $V_{ocI} = 1.06 \text{ V}, 1.06 \text{ V}, 1.07 \text{ V}$ , respectively. (3) In Table 5p, for  $p^+ - n$  X(x) –alloy junction solar cell and for  $r_{Cd(Sn)}$ -radius, with increasing  $x=(0, 0.5, 1)$ , one obtains with increasing  $x=(0, 0.5, 1)$ :  $\eta_{II_{max.}(\lambda)} = 32.51\%$ , 32.51%, 33.07%, according to  $T_H(\lambda) = 444.5 \text{ K}, 444.5 \text{ K}, 448.2 \text{ K}$ , at  $V_{ocII}(\text{V}) [ > V_{ocI}(\text{V}) ] = 1.17 \text{ V}, 1.18 \text{ V}, 1.20 \text{ V}$ , respectively, suggesting that such  $\eta_{I_{max.}(\lambda)}$ -and- $T_H$  variations depend on  $V_{ocII}(\text{V}) [ > V_{ocI}(\text{V}) ]$  – ones. (4) Finally, as discussed in above remarks (2) and (3), for  $x=1$ , the  $\text{GaP}_{1-x}\text{As}_x$  –alloy becomes the GaAs-one, and therefore,  $\eta_{I_{max.}}=31.15 \%$  and  $\eta_{II_{max.}}=33.07 \%$ , which can be compared with the corresponding results obtained by Moon et al.<sup>[6]</sup> and Green et al.<sup>[4]</sup> for the single-junction GaAs thin-film solar cell, 22.08 % and 29.71 %, respectively, suggesting that in order to obtain the highest efficiencies, the  $\text{GaP}_{1-x}\text{As}_x$ -alloy junction solar cells could be chosen rather than the crystalline GaAs-junction solar cell.

**KEYWORDS:** single  $\text{GaP}_{1-x}\text{As}_x$ -alloy junction solar cell; single crystalline GaAs-junction solar cell; photovoltaic conversion factor; photovoltaic conversion efficiency.

## INTRODUCTION

In single  $n^+(p^+) - p(n)$  X( $\equiv \text{GaP}_{1-x}\text{As}_x$ )-alloy junction solar cells at 300 K,  $0 \leq x \leq 1$ , by basing on the same physical model and treatment method, as used in our two recent works<sup>[1,2]</sup>, and also on other ones [2-11], we will investigate the highest (or maximal) efficiencies,  $\eta_{I_{max.}(\lambda)}$ , according to highest hot reservoir temperatures  $T_H(\text{K})$ , obtained from the Carnot- efficiency theorem, being proved by the entropy law.

In the following, we will show that the energy-band-structure parameters, due to the effects of x-concentration, size impurity, temperature T and heavy doping, affect strongly the dark (or total) minority-carrier saturation current density and the photovoltaic conversion effect.

## ENERGY BAND STRUCTURE PARAMETERS

### A. Effect of x- concentration

In the  $n^+(p^+) - p(n)$  single  $n^+(p^+) - p(n)$  X(x)- alloy junction at  $T=0 \text{ K}$ , the energy-band-structure parameters<sup>[1]</sup>, are expressed as functions of x, are given in the following.

(i)-The unperturbed relative effective electron (hole) mass in conduction (valence) bands are given by:

$$m_c(x)/m_o = 0.066 \times x + 0.13 \times (1 - x), \text{ and} \\ m_v(x)/m_o = 0.291 \times x + 0.5 \times (1 - x), \quad (1)$$

so that one obtains:  $m_c(x = 1)/m_o = (m_{c(\text{GaAs})}/m_o) = 0.066$ ,  
 $m_v(x = 1)/m_o = (m_{v(\text{GaAs})}/m_o) = 0.291$ , and  $m_c(x = 0)/m_o = (m_{c(\text{GaP})}/m_o) = 0.13$ ,  
 $m_v(x = 0)/m_o = (m_{v(\text{GaP})}/m_o) = 0.5$ .

(ii)-The unperturbed relative static dielectric constant of the intrinsic of the single crystalline X- alloy is found to be defined by:

$$\epsilon_o(x) = 13.13 \times x + 11.1 \times (1 - x), \quad (2)$$

which gives:  $\epsilon_o(x = 1) = \epsilon_{\text{GaAs}} = 13.13$ , and  $\epsilon_o(x = 0) = \epsilon_{\text{GaP}} = 11.1$ .

(iii)-Finally, the unperturbed band gap at 0 K is found to be given by:

$$E_{go}(x) \text{ in eV} = 1.52 \times x + 1.796 \times (1 - x), \quad (3)$$

giving rise to:  $E_{gio}(x = 1) = E_{g\text{GaAs}} = 1.52 \text{ eV}$ , and  $E_{gio}(x = 0) = E_{g\text{GaP}} = 1.796 \text{ eV}$ .

Therefore, we can define the effective donor (acceptor)-ionization energy, at  $r_{d(a)} = r_{do(ao)} = r_{p(\text{Ga})} = 0.11 \text{ nm}$  (0.126 nm), in absolute values as:

$$E_{do(ao)}(x) = \frac{13600 \times [m_{c(v)}(x)/m_o]}{[\epsilon_o(x)]^2} \text{ meV}, \quad (4)$$

and then, the isothermal bulk modulus, by:

$$B_{do(ao)}(x) \equiv \frac{E_{do(ao)}(x)}{\left(\frac{4\pi}{3}\right) \times (r_{do(ao)})^3}. \quad (5)$$

## B. Effects of Impurity-size, with a given x

Here, the effects of  $r_{d(a)}$  and x- concentration affect the changes in all the energy-band-structure parameters, expressed in terms of the effective relative dielectric constant  $\epsilon(r_{d(a)}, x)$ , in the following.

At  $r_{d(a)} = r_{do(ao)}$ , the needed boundary conditions are found to be, for the impurity-atom volume  $V = (4\pi/3) \times (r_{d(a)})^3$ ,  $V_{do(ao)} = (4\pi/3) \times (r_{do(ao)})^3$ , for the pressure  $p$ ,  $p_o = 0$ , and for the deformation potential energy (or the strain energy)  $\sigma$ ,  $\sigma_o = 0$ . Further, the two important equations (Van Cong et al., 1984), used to determine the  $\sigma$ -variation,  $\Delta\sigma \equiv$

$\sigma - \sigma_0 = \sigma$ , are defined by:  $\frac{dp}{dv} = -\frac{B}{v}$  and  $p = -\frac{d\sigma}{dv}$ . giving:  $\frac{d}{dv}\left(\frac{d\sigma}{dv}\right) = \frac{B}{v}$ . Then, by an integration, one gets:

$$[\Delta\sigma(r_{d(a)}, x)]_{n(p)} = B_{do(ao)}(x) \times (V - V_{do(ao)}) \times \ln\left(\frac{v}{v_{do(ao)}}\right) = E_{do(ao)}(x) \times \left[\left(\frac{r_{d(a)}}{r_{do(ao)}}\right)^3 - 1\right] \times \ln\left(\frac{r_{d(a)}}{r_{do(ao)}}\right) \geq 0. (6)$$

Furthermore, we also shown that, as  $r_{d(a)} > r_{do(ao)}$  ( $r_{d(a)} < r_{do(ao)}$ ), the compression (dilatation) gives rise to the increase (the decrease) in the energy gap  $E_{gn(gp)}(r_{d(a)}, x)$ , and the effective donor (acceptor)-ionization energy  $E_{d(a)}(r_{d(a)}, x)$  in absolute values, obtained in the effective Bohr model, which is represented respectively by:  $\pm [\Delta\sigma(r_{d(a)}, x)]_{n(p)}$ ,

$$E_{gn(gp)}(r_{d(a)}, x) - E_{go}(x) = E_{d(a)}(r_{d(a)}, x) - E_{do(ao)}(x) = E_{do(ao)}(x) \times \left[\left(\frac{\epsilon_0(x)}{\epsilon(r_{d(a)})}\right)^2 - 1\right] = + [\Delta\sigma(r_{d(a)}, x)]_{n(p)},$$

for  $r_{d(a)} \geq r_{do(ao)}$ , and for  $r_{d(a)} \leq r_{do(ao)}$ ,

$$E_{gn(gp)}(r_{d(a)}, x) - E_{go}(x) = E_{d(a)}(r_{d(a)}, x) - E_{do(ao)}(x) = E_{do(ao)}(x) \times \left[\left(\frac{\epsilon_0(x)}{\epsilon(r_{d(a)})}\right)^2 - 1\right] = - [\Delta\sigma(r_{d(a)}, x)]_{n(p)}. (7)$$

Therefore, from Equations (6) and (7), one obtains the expressions for relative dielectric constant  $\epsilon(r_{d(a)}, x)$  and energy band gap  $E_{gn(gp)}(r_{d(a)}, x)$ , as:

(i)-for  $r_{d(a)} \geq r_{do(ao)}$ , since  $\epsilon(r_{d(a)}, x) = \frac{\epsilon_0(x)}{\sqrt{1 + \left[\left(\frac{r_{d(a)}}{r_{do(ao)}}\right)^3 - 1\right] \times \ln\left(\frac{r_{d(a)}}{r_{do(ao)}}\right)^3}} \leq \epsilon_0(x)$ ,

$$E_{gn(gp)}(r_{d(a)}, x) - E_{go}(x) = E_{d(a)}(r_{d(a)}, x) - E_{do(ao)}(x) = E_{do(ao)}(x) \times \left[\left(\frac{r_{d(a)}}{r_{do(ao)}}\right)^3 - 1\right] \times \ln\left(\frac{r_{d(a)}}{r_{do(ao)}}\right)^3 \geq 0, (8a)$$

according to the increase in both  $E_{gn(gp)}(r_{d(a)}, x)$  and  $E_{d(a)}(r_{d(a)}, x)$ , for a given  $x$ , and

(ii)-for  $r_{d(a)} \leq r_{do(ao)}$ , since  $\epsilon(r_{d(a)}, x) = \frac{\epsilon_0(x)}{\sqrt{1 - \left[\left(\frac{r_{d(a)}}{r_{do(ao)}}\right)^3 - 1\right] \times \ln\left(\frac{r_{d(a)}}{r_{do(ao)}}\right)^3}} \geq \epsilon_0(x)$ , with a condition,

given by:  $\left[\left(\frac{r_{d(a)}}{r_{do(ao)}}\right)^3 - 1\right] \times \ln\left(\frac{r_{d(a)}}{r_{do(ao)}}\right)^3 < 1$ ,

$$E_{gn(gp)}(r_{d(a)}, x) - E_{go}(x) = E_{d(a)}(r_{d(a)}, x) - E_{do(ao)}(x) = -E_{do(ao)}(x) \times \left[\left(\frac{r_{d(a)}}{r_{do(ao)}}\right)^3 - 1\right] \times \ln\left(\frac{r_{d(a)}}{r_{do(ao)}}\right)^3 \leq 0, (8b)$$

corresponding to the decrease in both  $E_{gn(gp)}(r_{d(a)}, x)$  and  $E_{d(a)}(r_{d(a)}, x)$ , for a given  $x$ .

Furthermore, it is interesting to remark that the critical total donor (acceptor)-density in the metal-insulator transition (MIT) at  $T=0$  K,  $N_{CDn(CDp)}(r_{d(a)}, x)$ , was given by the Mott's criterium, as:

$$N_{CDn(CDp)}(r_{d(a)}, x)^{1/3} \times a_{Bn(Bp)}(r_{d(a)}, x) = M_{n(p)}, M_{n(p)} = 0.25, (9a)$$

which can be explained from the definition of the reduced effective Wigner-Seitz (WS) radius  $r_{sn(sp)}$ , characteristic of interactions, by:

$$r_{sn(sp)}(N, r_{d(a)}, x) \equiv \left(\frac{3}{4\pi N}\right)^{1/3} \times \frac{1}{a_{Bn(Bp)}(r_{d(a)}, x)} = 1.1723 \times 10^8 \times \left(\frac{1}{N}\right)^{1/3} \times \frac{m_{c(v)}(x)/m_0}{\varepsilon(r_{d(a)}, x)}, \quad (9b)$$

being equal to, in particular, at  $N=N_{CDn(CDp)}(r_{d(a)}, x)$ :  $r_{sn(sp)}(N_{CDn(CDp)}(r_{d(a)}, x), r_{d(a)}, x) = 2.4814$ , for any  $(r_{d(a)}, x)$ -values. So, from Eq. (9b), one has:

$$N_{CDn(CDp)}(r_{d(a)}, x)^{1/3} \times a_{Bn(Bp)}(r_{d(a)}, x) = \left(\frac{3}{4\pi}\right)^{1/3} \times \frac{1}{2.4814} = 0.25 = (WS)_{n(p)} = M_{n(p)}. \quad (9c)$$

In our recent paper<sup>[1]</sup>, we have also showed that  $N_{CDn(CDp)}$  is just the density of electrons (holes) localized in the exponential conduction (valence)-band tail (EBT), with a precision of the order of  $2.92 \times 10^{-7}$ . So, the density of electrons (holes) given in parabolic conduction (valence) bands can be defined by:

$$N^*(N, r_{d(a)}, x) \equiv N - N_{CDn(CDp)}(r_{d(a)}, x), \quad (9d)$$

which will be used in the n(p)-type degenerate X(x)-alloy, as follows.

### C. Effect of temperature T, with given x and $r_{d(a)}$

Here, the intrinsic band gap  $E_{gin(gip)}(r_{d(a)}, x, T)$  at any T is given by:

$$E_{gin(gip)}(r_{d(a)}, x, T) \text{ in eV} = E_{gn(gp)}(r_{d(a)}, x) - 10^{-4} \times T^2 \times \left[ \frac{5.405 \times x}{T+204} + \frac{3.065 \times (1-x)}{T+94} \right], \quad (10)$$

Which gives:  $E_{gin(gip)}(r_{do(ao)}, x = 0, T = 0K) = 1.796 \text{ eV}$  and  $E_{gin(gip)}(r_{do(ao)}, x = 1, T = 0K) = 1.52 \text{ eV}$ ,

and  $E_{gin(gip)}(r_{do(ao)}, x = 0, T = 300 \text{ K}) = 1.72599 \text{ eV}$  and

$E_{gin(gip)}(r_{do(ao)}, x = 1, T = 300 \text{ K}) = 1.42348 \text{ eV}$ , suggesting that, for given x and  $r_{d(a)}$ ,

$E_{gin(gip)}$  decreases with an increasing T, as observed in next Table 1 in Appendix 1.

Furthermore, in the n(p)-type X(x)-alloy, one can define the intrinsic carrier concentration

$$n_{in(ip)} \text{ by: } n_{in(ip)}^2(r_{d(a)}, x, T) \equiv N_c(T, x) \times N_v(T, x) \times \exp\left(\frac{-E_{gin(gip)}(r_{d(a)}, x, T)}{k_B T}\right), \quad (11)$$

where  $N_{c(v)}(T, x)$  is the conduction (valence)-band density of states, being defined as:

$$N_{c(v)}(T, x) = 2 \times \left(\frac{m_{c(v)}(x) \times k_B T}{2\pi \hbar^2}\right)^{3/2} (\text{cm}^{-3}).$$

### D. Heavy Doping Effect, with given T, x and $r_{d(a)}$

Here, as given in our previous works<sup>[1,2]</sup>, the Fermi energy  $E_{Fn}(-E_{Fp})$ , band gap narrowing (BGN), and apparent band gap narrowing (ABGN), are reported in the following.

First, the reduced Fermi energy  $\eta_{n(p)}$  or the Fermi energy  $E_{Fn}(-E_{Fp})$ , obtained for any T and any effective d(a)-density,  $N^*(N, r_{d(a)}, x) = N^*$ , defined in Eq. (9d), for a simplicity of presentation, being investigated in our previous paper<sup>[8]</sup>, with a precision of the order of  $2.11 \times 10^{-4}$ , is found to be given by:

$$\eta_{n(p)}(u) \equiv \frac{E_{Fn}(u)}{k_B T} \left( \frac{-E_{Fp}(u)}{k_B T} \right) = \frac{G(u) + Au^B F(u)}{1 + Au^B}, \quad A = 0.0005372 \text{ and } B = 4.82842262, \quad (12)$$

where u is the reduced electron density,  $u(N^*, T, x) \equiv \frac{N^*}{N_{c(v)}(T, x)}$ ,  $F(u) = au^{\frac{2}{3}} \left( 1 + bu^{-\frac{4}{3}} + cu^{-\frac{8}{3}} \right)^{-\frac{2}{3}}$ ,  
 $a = [(3\sqrt{\pi}/4) \times u]^{2/3}$ ,  $b = \frac{1}{8} \left( \frac{\pi}{a} \right)^2$ ,  $c = \frac{62.3739855}{1920} \left( \frac{\pi}{a} \right)^4$ , and  $G(u) \simeq \text{Ln}(u) + 2^{-\frac{3}{2}} \times u \times e^{-du}$ ,  
 $d = 2^{3/2} \left[ \frac{1}{\sqrt{27}} - \frac{a}{16} \right] > 0$ .

Here, one notes that: (i) as  $u \gg 1$ , according to the HD [d(a)- X(x)- alloy] ER-case, or to the degenerate case, Eq. (12) is reduced to the function F(u), and (ii)  $\frac{E_{Fn}(u \ll 1)}{k_B T} \left( \frac{-E_{Fp}(u \ll 1)}{k_B T} \right) \ll -1$ , to the LD [a(d)- X(x)- alloy] BR-case, or to the non-degenerate case, Eq. (12) is reduced to the function G(u). Here, the notations: HD(LD) and ER(BR), mean: heavily doped (lightly doped)-cases and emitter (base)-regions, respectively.

So, the numerical results of  $B_{do(ao)}$ ,  $\epsilon$ ,  $E_{gno(gpo)}$ ,  $N_{CDn(CDp)}$ ,  $E_{gin(gip)}(r_{d(a)}, x, T)$ , and  $\eta_{n(p)}(u)$ , calculated using Equations (5), (8a, 8b), (9a), (10), and (12), respectively.

**Table 1 in Appendix 1**

Now, if denoting now the effective Wigner-Seitz radius  $r_{sn(sp)}$ , characteristic of the interactions, by:

$$r_{sn(sp)}(N^*, r_{d(a)}, x) = 1.1723 \times 10^8 \times \left( \frac{1}{N^*} \right)^{1/3} \times \frac{m_{c(v)}(x)}{\epsilon(r_{d(a)}, x)}, \quad (13)$$

the correlation energy of an effective electron gas,  $E_{cn(cp)}(N^*, r_{d(a)}, x)$ , is given as<sup>[4]</sup>:

$$E_{cn(cp)}(N^*, r_{d(a)}, x) = \frac{-0.87553}{0.0908 + r_{sn(sp)}} + \frac{\frac{0.87553}{0.0908 + r_{sn(sp)}} + \left( \frac{2[1 - \ln(2)]}{\pi^2} \right) \times \ln(r_{sn(sp)}) - 0.093288}{1 + 0.03847728 \times r_{sn(sp)}^{1.67378876}}.$$

Now, taking into account various spin-polarized chemical potential-energy contributions such as (Van Cong, 2024): exchange energy of an effective electron (hole) gas, majority-carrier correlation energy of an effective electron (hole) gas, minority hole (electron) correlation energy, majority electron (hole)-ionized d(a) interaction screened Coulomb potential energy,



and finally minority hole (electron)-ionized d(a) interaction screened Coulomb potential energy, the band gap narrowing (BGN) are given as follows.

Thus, in the n-type HD X(x)- alloy, the BGN is found to be given by<sup>[2]</sup>:

$$\Delta E_{gn}(N^*, r_d, x) \simeq a_1 \times \frac{\varepsilon_0(x)}{\varepsilon(r_d, x)} \times N_r^{1/3} + a_2 \times \frac{\varepsilon_0(x)}{\varepsilon(r_d, x)} \times N_r^{1/3} \times (2.503 \times [-E_{cn}(r_{sn}) \times r_{sn}]) + a_3 \times \left[ \frac{\varepsilon_0(x)}{\varepsilon(r_d, x)} \right]^{5/4} \times \sqrt{\frac{m_v}{m_c}} \times N_r^{1/4} + a_4 \times \sqrt{\frac{\varepsilon_0(x)}{\varepsilon(r_d, x)}} \times N_r^{1/2} \times 2 + a_5 \times \left[ \frac{\varepsilon_0(x)}{\varepsilon(r_d, x)} \right]^2 \times N_r^{1/6}$$

$$N_r \equiv \left( \frac{N^*}{N_{CDn}(r_d, x)} \right), \quad (14n)$$

Where  $a_1 = 3.8 \times 10^{-3}$  (eV),  $a_2 = 6.5 \times 10^{-4}$  (eV),  $a_3 = 2.8 \times 10^{-3}$  (eV),  $a_4 = 5.597 \times 10^{-3}$  (eV) and  $a_5 = 8.1 \times 10^{-4}$  (eV), and in the p-type HD X(x)- alloy, as:

$$\Delta E_{gp}(N^*, r_a, x) \simeq a_1 \times \frac{\varepsilon_0(x)}{\varepsilon(r_a, x)} \times N_r^{1/3} + a_2 \times \frac{\varepsilon_0(x)}{\varepsilon(r_a, x)} \times N_r^{1/3} \times (2.503 \times [-E_{cp}(r_{sp}) \times r_{sp}]) + a_3 \times \left[ \frac{\varepsilon_0(x)}{\varepsilon(r_a, x)} \right]^{5/4} \times \sqrt{\frac{m_c}{m_v}} \times N_r^{1/4} + 2a_4 \times \sqrt{\frac{\varepsilon_0(x)}{\varepsilon(r_a, x)}} \times N_r^{1/2} + a_5 \times \left[ \frac{\varepsilon_0(x)}{\varepsilon(r_a, x)} \right]^2 \times N_r^{1/6}$$

$$N_r \equiv \left( \frac{N^*}{N_{CDp}(r_a, x)} \right), \quad (14p)$$

Where  $a_1 = 3.15 \times 10^{-3}$  (eV),  $a_2 = 5.41 \times 10^{-4}$  (eV),  $a_3 = 2.32 \times 10^{-3}$  (eV),  $a_4 = 4.195 \times 10^{-3}$  (eV) and  $a_5 = 9.80 \times 10^{-5}$  (eV).

Therefore, in the HD[d(a)- X(x)- alloy] ER, we can define the effective extrinsic carrier concentration,  $n_{en(ep)}^*$ , by :

$$n_{en(ep)}^*(N^*, T, r_{d(a)}, x) \equiv \sqrt{N^* \times p_o(n_o)} = n_{in(ip)}(T, r_{d(a)}, x) \times \exp \left[ \frac{\Delta E_{agn(agp)}}{2k_B T} \right], \quad (15)$$

where the apparent band gap narrowing (ABGN),  $\Delta E_{agn(agp)}$ , is defined by:

$$\Delta E_{agn}(N^*, T, r_d, x) \equiv \Delta E_{gn}(N^*, r_d, x) + k_B T \times \ln \left( \frac{N^*}{N_c(T, x)} \right) - E_{Fn}(N^*, T, x), \quad (16n)$$

$$\Delta E_{agp}(N^*, T, r_a, x) \equiv \Delta E_{gp}(N^*, r_a, x) + k_B T \times \ln \left( \frac{N^*}{N_v(T, x)} \right) + E_{Fp}(N^*, T, x). \quad (16p)$$

### TOTAL MINORITY-CARRIER SATURATION CURRENT DENSITY

In the two  $n^+(p^+) - p(n)$  X(x)- alloy -junction solar cells, denoted respectively by I(II), the total carrier-minority saturation current density is defined by:

$$J_{oI(oII)} \equiv J_{Eno(Epo)} + J_{Bpo(Bno)} \quad (17)$$

where  $J_{Bpo(Bno)}$  is the minority-electron (hole) saturation current density injected into the LD[a(d)- X(x)- alloy] BR, and  $J_{Eno(Epo)}$  is the minority-hole (electron) saturation-current density injected into the HD[d(a)- X(x)- alloy] ER.

**J<sub>Bpo(Bno)</sub> in the LD[a(d)- X(x)- alloy]BR**

Here, J<sub>Bpo(Bno)</sub> is determined by<sup>[2]</sup>:

$$J_{Bpo(Bno)}(N_{a(d)}, T, r_{a(d)}, x) = \frac{e \times n_{ip(in)}^2(T, r_{a(d)}, x) \times \sqrt{\frac{D_{e(h)}(N_{a(d)}, T, r_{a(d)}, x)}{\tau_{eB(hB)}(N_{a(d)})}}}{N_{a(d)}}, \tag{18}$$

where  $n_{ip(in)}^2(T, r_{d(a)}, x)$  is determined Eq. (11),  $D_{e(h)}(N_{a(d)}, T, r_{a(d)}, x)$  is the minority electron (minority hole) diffusion coefficient:

$$D_e(N_a, T, r_a, x) = \frac{k_B T}{e} \times \left[ 200 + \frac{8300}{1 + \left(\frac{N_a}{1.3 \times 10^{17} \text{ cm}^{-3}}\right)^{0.91}} \right] \times \left(\frac{\varepsilon(r_a, x)}{\varepsilon_0(x)}\right)^2 \text{ (cm}^2\text{s}^{-1}\text{)}, \tag{19a}$$

$$D_h(N_d, T, r_d, x) = \frac{k_B T}{e} \times \left[ 130 + \frac{270}{1 + \left(\frac{N_d}{8 \times 10^{17} \text{ cm}^{-3}}\right)^{1.23}} \right] \times \left(\frac{\varepsilon(r_d, x)}{\varepsilon_0(x)}\right)^2 \text{ (cm}^2\text{s}^{-1}\text{)}, \tag{19b}$$

and  $\tau_{eB(hB)}(N_{a(d)})$  is the minority electron (minority hole) lifetime in the BR:

$$\tau_{eB}(N_a)^{-1} = \frac{1}{10^{-7}} + 3 \times 10^{-13} \times N_a + 1.83 \times 10^{-31} \times N_a^2, \tag{20a}$$

$$\tau_{hB}(N_d)^{-1} = \frac{1}{10^{-7}} + 11.76 \times 10^{-13} \times N_d + 2.78 \times 10^{-31} \times N_d^2. \tag{20b}$$

**J<sub>Eno(Epo)</sub> in the HD[d(a)- X(x)- alloy]ER**

In the non-uniformly and heavily doped emitter region of d(a)- X(x) devices, the effective Gaussian d(a)-density profile or the d(a) (majority-e(h)) density, is defined in such the HD[d(a)- X(x) alloy] ER-width W, as<sup>[2]</sup>:

$$\rho_{d(a)}(y, N^*, W) = N_{d(a)} \times \exp\left\{-\left(\frac{y}{W}\right)^2 \times \ln\left[\frac{N^*}{N_{do(ao)}(W)}\right]\right\} \equiv N^* \times \left[\frac{N^*}{N_{do(ao)}(W)}\right]^{-\left(\frac{y}{W}\right)^2}, \quad 0 \leq y \leq W,$$

$$N_{do(ao)}(W) \equiv 7.9 \times 10^{17} (2 \times 10^5) \times \exp\left\{-\left(\frac{W}{184.2(1) \times 10^{-7} \text{ cm}}\right)^{1.066(0.5)}\right\} \text{ (cm}^{-3}\text{)}, \tag{21}$$

where  $\rho_{d(a)}(y = 0) = N^*$  is the surface d(a)-density, and at the emitter-base junction,  $\rho_{d(a)}(y = W) = N_{do(ao)}(W)$ , which decreases with increasing W. Further, the “effective doping density” is defined by:

$$N_{d(a)}^*(y, N^*, T, r_{d(a)}, x) \equiv \rho_{d(a)}(y) / \exp\left[\frac{\Delta E_{agn(agg)}(\rho_{d(a)}, T, r_{d(a)}, x)}{k_B T}\right],$$

$$N_{d(a)}^*(y = 0, N^*, T, r_{d(a)}, x) \equiv \frac{N^*}{\exp\left[\frac{\Delta E_{agn(agg)}(N^*, T, r_{d(a)}, x)}{k_B T}\right]}, \text{ and}$$

$$N_{d(a)}^*(y = W, T, r_{d(a)}, x) \equiv \frac{N_{do(ao)}(W)}{\exp\left[\frac{\Delta E_{agn(agg)}(N_{do(ao)}(W), T, r_{d(a)}, x)}{k_B T}\right]}, \tag{22}$$



where the apparent band gap narrowing  $\Delta E_{agn(agg)}$  is determined in Equations (16n, 16p), replacing  $N^*$  by  $\rho_{d(a)}(y, N^*, W)$ .

Now, we can define the minority hole (minority electron) transport parameter  $F_{h(e)}$ , as:

$$F_{h(e)}(y, N^*, T, r_{d(a)}, x) \equiv \frac{N^*}{D_{h(e)} \times \exp\left[\frac{\Delta E_{agn(agg)}}{k_B T}\right]} \quad (\text{cm}^{-5} \times \text{s}), \quad (23)$$

being related to the minority hole (electron) diffusion length,  $L_{h(e)}(y, N^*, T, r_{d(a)}, x)$ , as:

$$L_{h(e)}^{-2}(y, N^*, T, r_{d(a)}, x) = [\tau_{hE(eE)} \times D_{h(e)}]^{-1} = (C \times F_{h(e)})^2 = \left(C \times \frac{N_{d(a)}^*}{D_{h(e)}}\right)^2 = \left(C \times \frac{n_{in(ip)}^2(T, r_{d(a)})}{p_o(n_o) \times D_{h(e)}}\right)^2,$$

where the constant C was chosen to be equal to:  $2.0893 \times 10^{-30} \text{ (cm}^4/\text{s)}$ , and finally the minority hole (minority electron) lifetime  $\tau_{hE(eE)}$ , by:

$$\tau_{hE(eE)} \equiv \frac{1}{D_{h(e)} \times L_{h(e)}^{-2}} = \frac{1}{D_{h(e)} \times (C \times F_{h(e)})^2}. \quad (24)$$

Then, under low-level injection, in the absence of external generation, and for the steady-state case, we can define the minority-h(e) density by:

$$p_o(y)[n_o(y)] \equiv \frac{n_{in(ip)}^2}{N_{d(a)}^*(y=W, T, r_{d(a)}, x)}, \quad (25)$$

and a normalized excess minority-h(e) density  $u(x)$  or a relative deviation between  $p(y)[n(y)]$  and  $p_o(y)[n_o(y)]$ .

$$u(y) \equiv \frac{p(y)[n(y)] - p_o(y)[n_o(y)]}{p_o(y)[n_o(y)]}, \quad (26)$$

which must verify the two following boundary conditions as:

$$u(y = 0) \equiv \frac{-J_h(y=0)[J_e(y=0)]}{eS \times p_o(y=0)[n_o(y=0)]},$$

$$u(y = W) = \exp\left(\frac{V}{n_{I(II)}(V) \times V_T}\right) - 1.$$

Here,  $n_{I(II)}(V)$  is the photovoltaic conversion factor, being determined later,  $S \left(\frac{\text{cm}}{\text{s}}\right)$  is the surface recombination velocity at the emitter contact,  $V$  is the applied voltage,  $V_T \equiv (k_B T/e)$  is the thermal voltage, and the minority-hole (electron) current density  $J_{h(e)}(y, r_{d(a)}, x)$ .

Further, from the Fick's law for minority hole (electron)-diffusion equations, one has<sup>[1,2]</sup>:

$$J_{h(e)}(y, N^*, T, r_{d(a)}, x) = \frac{-e(+e) \times n_{in(ip)}^2}{F_{h(e)}(y)} \times \frac{du(y)}{dy} = \frac{-e(+e) n_{in(ip)}^2 D_{h(e)}(N^*, r_{d(a)}, x)}{N_{d(a)}^*(y, N^*, T, r_{d(a)}, x)} \times \frac{du(y)}{dy}, \quad (27)$$

where  $N_{d(a)}^*(y, r_{d(a)}, x)$  is given in Eq. (22),  $D_{h(e)}$  and  $F_{h(e)}$  are determined respectively in Equations (19) and (23), and from the minority-hole (electron) continuity equation as:

$$N_{d(a)}^*(y, N^*, T, r_{d(a)}, x)$$

$$\frac{dJ_{h(e)}(y, N^*, T, r_{d(a)}, x)}{dy} = -e(+e) \times n_{in(p)}^2 \times \frac{u(y)}{F_{h(e)}(y) \times L_{h(e)}^2(y)} = -e(+e) \times n_{in(p)}^2 \times \frac{u(y)}{N_{d(a)}^*(y, N^*, T, r_{d(a)}, x) \times \tau_{h(eE)}}, \quad (28)$$

Therefore, the following second-order differential equation is obtained:

$$\frac{d^2 u(y)}{dy^2} - \frac{dF_{h(e)}(y)}{dy} \times \frac{du(y)}{dy} - \frac{u(y)}{L_{h(e)}^2(y)} = 0, \quad (29)$$

Then, taking into account the two above boundary conditions given in Eq. (26), one thus gets the general solution of this Eq. (29), as:

$$u(y) = \frac{\sinh(P(y)) + I(W, S) \times \cosh(P(y))}{\sinh(P(W)) + I(W, S) \times \cosh(P(W))} \times \left( \exp\left(\frac{v}{n_{i(I)}(V) \times V_T}\right) - 1 \right), \quad (30)$$

where the factor  $I(W, S)$  is determined by:  $D_{h(e)}(N_d, T, r_{d(a)}, x)$

$$I(T, r_{d(a)}, x, W, S) = \frac{D_{h(e)}(y=W, N_{do(ao)}(W), T, r_{d(a)}, x)}{S \times L_{h(e)}(y=W, N_{do(ao)}(W), T, r_{d(a)}, x)}. \quad (31)$$

Further, since  $\frac{dP(y)}{dy} \equiv C \times F_{h(e)}(y) = \frac{1}{L_{h(e)}(x)}$ ,  $C = 2.0893 \times 10^{-30}$  (cm<sup>4</sup>/s), for the X(x)-alloy,

being an empirical parameter, chosen for each crystalline semiconductor,  $P(y)$  is thus found to be defined by:  $P(y) \equiv \int_0^y \frac{dy}{L_{h(e)}(y)}$ ,  $0 \leq y \leq W$ ,  $P(y=W) \equiv \left(\frac{1}{W} \times \int_0^W \frac{dy}{L_{h(e)}(y)}\right) \times W \equiv \frac{W}{L_{h(e)}^*(y)} = \frac{L_{h(e)}(y)}{L_{h(e)}^*(y)} \times \frac{W}{L_{h(e)}(y)}$ , (32)

where  $L_{h(e)}^*(y)$  is the effective minority hole (minority electron) diffusion length. Further, the minority-hole (electron) current density injected into the HD[d(a)- X(x) alloy] ER is found to be given by:  $J_{h(e)}(y, W, N^*, T, r_{d(a)}, x, S, V) = -J_{Eno}(y, W, N^*, T, r_{d(a)}, x, S) \left[ J_{Epo}(y, W, N^*, T, r_{d(a)}, x, S) \times \left( \exp\left(\frac{v}{n_{i(I)}(V) \times V_T}\right) - 1 \right) \right]$ , (33)

where  $J_{Eno}(Epo)$  is the saturation minority hole (minority electron) current density,

$$J_{Eno}(Epo)(y, W, N^*, T, r_{d(a)}, x, S) = \frac{en_{in(ip)}^2 \times D_{h(e)}}{N_{d(a)}^*(y, N^*, T, r_{d(a)}, x) \times L_{h(e)}} \times \frac{\cosh(P(x)) + I(W, S) \times \sinh(P(x))}{\sinh(P(W)) + I(W, S) \times \cosh(P(W))}. \quad (34)$$

In the following, we will denote  $P(W)$  and  $I(W, S)$  by  $P$  and  $I$ , for a simplicity. So, Eq. (30) gives:

$$J_{Eno}(Epo)(y=0, W, N^*, T, r_{d(a)}, x, S) = \frac{en_{in(ip)}^2 \times D_{h(e)}}{N_{d(a)}^*(y, N^*, T, r_{d(a)}, x) \times L_{h(e)}} \times \frac{1}{\sinh(P) + I \times \cosh(P)} \quad (35)$$

$$J_{Eno}(Epo)(y=W, W, N^*, T, r_{d(a)}, x, S) = \frac{en_{in(ip)}^2 \times D_{h(e)}}{N_{d(a)}^*(y=W, N^*, T, r_{d(a)}, x) \times L_{h(e)}} \times \frac{\cosh(P) + I \times \sinh(P)}{\sinh(P) + I \times \cosh(P)}, \quad (36)$$

and then,

$$\frac{J_{h(e)}(y=0, W, N^*, T, r_{d(a)}, x, S, V)}{J_{h(e)}(y=W, W, N^*, T, r_{d(a)}, x, S, V)} \equiv \frac{J_{Eno}(Epo)(y=0, W, N^*, T, r_{d(a)}, x, S)}{J_{Eno}(Epo)(y=W, W, N^*, T, r_{d(a)}, x, S)} = \frac{1}{\cosh(P) + I \times \sinh(P)} \quad (37)$$

Now, if defining the effective excess minority-hole (electron) charge storage in the emitter region by:

$$Q_{h(e)}^*(y=W, N^*, T, r_{d(a)}, x) \equiv \int_0^W +e(-e) \times u(y) \times p_o(y) [n_o(y)] \times \frac{\tau_{h(eE)}(N^*, T, r_{d(a)}, x)}{\tau_{h(eE)}(\rho_{d(a)}(x), T, r_{d(a)}, x)} dy, \quad \text{and}$$

the effective minority hole (minority electron) transit time [htt(ett)] by:

$\tau_{\text{htt(ett)}}^{\#}(y = W, W, N^*, r_{d(a)}, x, S) \equiv Q_{h(e)}^{\#}(y = W, N^*, T, r_{d(a)}, x) / J_{\text{Eno(Epo)}}(y = W, W, N^*, T, r_{d(a)}, x, S)$ , and from Equations (24, 31), one obtains:

$$\frac{\tau_{\text{htt(ett)}}^{\#}(y=W, W, N^*, T, r_{d(a)}, x, S)}{\tau_{hE(eE)}} \equiv 1 - \frac{J_{\text{Eno(Epo)}}(y=0, W, N^*, T, r_{d(a)}, x, S)}{J_{\text{Eno(Epo)}}(y=W, W, N^*, T, r_{d(a)}, x, S)} = 1 - \frac{1}{\cosh(P) + I \times \sinh(P)} \quad (38)$$

Now, some important results can be obtained and discussed below.

As  $P \ll 1$  (or  $W \ll L_{h(e)}$ ) and  $S \rightarrow \infty$ ,  $I \equiv I(W, S) = \frac{D_{h(e)}(N_{do(ao)}(W), T, r_{d(a)}, x)}{S \times L_{h(e)}(N_{do(ao)}(W), T, r_{d(a)}, x)} \rightarrow 0$ , from Eq. (38),

one has:  $\frac{\tau_{\text{htt(ett)}}^{\#}(y=W, W, N^*, T, r_{d(a)}, x, S)}{\tau_{hE(eE)}} \rightarrow 0$ , suggesting a completely transparent emitter region (CTER)-case, where, from Eq. (36), one obtains:

$$J_{\text{Eno(Epo)}}(y = W, N^*, T, r_{d(a)}, x, S \rightarrow \infty) \rightarrow \frac{en_{in(ip)}^2 \times D_{h(e)}}{N_{d(a)}^{\#}(y=W, N^*, T, r_{d(a)}, x) \times L_{h(e)}} \times \frac{1}{P(W)} \quad (39)$$

Further, as  $P \gg 1$  (or  $W \gg L_{h(e)}$ ) and  $S \rightarrow 0$ ,

$I \equiv I(y = W, r_{d(a)}, x, S) = \frac{D_{h(e)}(N_{do(ao)}(W), T, r_{d(a)}, x)}{S \times L_{h(e)}(N_{do(ao)}(W), T, r_{d(a)}, x)} \rightarrow \infty$ , and from Eq. (38) one has:

$\frac{\tau_{\text{htt(ett)}}^{\#}(y=W, W, N^*, T, r_{d(a)}, x, S)}{\tau_{hE(eE)}} \rightarrow 1$ , suggesting a completely opaque emitter region (COER)-case,

where, from Eq. (36), one gets:

$$J_{\text{Eno(Epo)}}(y = W, N^*, T, r_{d(a)}, x, S \rightarrow 0) \rightarrow \frac{en_{in(ip)}^2 \times D_{h(e)}}{N_{d(a)}^{\#}(y=W, N^*, T, r_{d(a)}, x) \times L_{h(e)}} \times \tanh(P) \quad (40)$$

In summary, in the two  $n^+(p^+) - p(n)$  X(x)-alloy junction solar cells, the dark carrier-minority saturation current density  $J_{oI(oII)}$ , defined in Eq. (17), is now rewritten as:

$$J_{oI(oII)}(W, N^*, T, r_{d(a)}, x, S; N_{a(d)}, r_{a(d)}, x) \equiv J_{\text{Eno(Epo)}}(W, N^*, T, r_{d(a)}, x, S) + J_{\text{Bpo(Bno)}}(N_{a(d)}, T, r_{a(d)}, x), \quad (41)$$

where  $J_{\text{Eno(Epo)}}$  and  $J_{\text{Bpo(Bno)}}$  are determined respectively in Equations (36, 18).

### PHOTOVOLTAIC CONVERSION EFFECT AT 300K

Here, in the  $n^+(p^+) - p(n)$  X(x) -alloy junction solar cells at  $T=300$  K, denoted respectively by  $I(II)$ , and for physical conditions, respectively, as:

$$W = 15 \mu\text{m}, N = 10^{20} \text{cm}^{-3} (10^{20} \text{cm}^{-3}), r_{d(a)}, x, S = 100 \left(\frac{\text{cm}}{\text{s}}\right); N_{a(d)} = 10^{17} \text{cm}^{-3}, r_{a(d)}, x, \quad (42)$$

we propose, at given open circuit voltages:  $V_{ocI1(ocI2)}$  and  $V_{ocII1(ocII2)}$ , the corresponding data of the short circuit current density  $J_{scI(II)}$ , in order to formulate our following treatment method of two fix points, as:

$$\text{at } V_{ocI1(ocI2)}(V) = 0.980 (1.1272), J_{scI1(scI2)}(\text{mA}/\text{cm}^2) = 27.06 (29.76),$$

$$\text{at } V_{ocII1(ocII2)}(V) = 0.980 (1.03), J_{scII1(scII2)}(\text{mA}/\text{cm}^2) = 24.2 (29.84). \quad (43)$$

Now, we define the net current density  $J$  at  $T=300$  K, obtained for the infinite shunt resistance, and expressed as a function of the applied voltage  $V$ , flowing through the  $n^+(p^+) - p(n)$   $X(x)$ -alloy junction of solar cells, as:

$$J(V) \equiv J_{ph.}(V) - J_{oi(oiI)} \times (e^{X_{I(II)}(V)} - 1), X_{I(II)}(V) \equiv \frac{V}{n_{I(II)}(V) \times V_T}, X_{I(II)}(V) \equiv \frac{V}{n_{I(II)}(V) \times V_T}, \quad (44)$$

where the function  $n_{I(II)}(V)$  is the photovoltaic conversion factor (PVCF), noting that as  $V = V_{oc}$ , being the open circuit voltage,  $J(V = V_{oc}) = 0$ , the photocurrent density is defined by:  $J_{ph.}(V = V_{oc}) \equiv J_{scI(scII)}(W, N^*, T, r_{d(a)}, x, S; N_{a(d)}, T, r_{a(d)}, x, V_{oc})$ , for  $V_{oc} \geq V_{ocI1(ocII1)}$ .

Therefore, the photovoltaic conversion effect occurs, according to:

$$J_{scI(scII)}(W, N^*, T, r_{d(a)}, x, S; N_{a(d)}, T, r_{a(d)}, x, V_{oc}) \equiv J_{oi(oiI)}(W, N^*, T, r_{d(a)}, x, S; N_{a(d)}, T, r_{a(d)}, x) \times (e^{X_{I(II)}(V_{oc})} - 1), \quad (45)$$

wheren $n_{I(II)}(V_{oc}) \equiv n_{I(II)}(W, N^*, T, r_{d(a)}, x, S; N_{a(d)}, r_{a(d)}, x, V_{oc})$ , and  $X_{I(II)}(V_{oc}) \equiv \frac{V_{oc}}{n_{I(II)}(V_{oc}) \times V_T}$ .

Here, one remarks that (i) for a given  $V_{oc}$ , both  $n_{I(II)}$  and  $J_{oi(oiI)}$  have the same variations, obtained in the same physical conditions, as observed in the following calculation, (ii) the function  $(e^{X_{I(II)}(V_{oc})} - 1)$  or the PVCF,  $n_{I(II)}$ , representing the photovoltaic conversion effect, converts the light, represented by  $J_{scI(scII)}$ , into the electricity, by  $J_{oi(oiI)}$ , and finally, for given  $(W, N^*, T, r_{d(a)}, x, S; N_{a(d)}, T, r_{a(d)}, x, V_{oc})$ -values,  $n_{I(II)}(V_{oc})$  is determined.

Now, for  $V_{oc} \geq V_{ocI1(ocII1)}$ , one can propose the general expressions for the PVCF, in order

to get exactly the values of  $n_{I1(II1)}(V_{ocI1(ocII1)})$  and  $n_{I2(II2)}(V_{ocI2(ocII2)})$ , as functions of  $V_{oc}$ ,

$$\text{by: } n_{I(II)}(W, N^*, T, r_{d(a)}, x, S; N_{a(d)}, T, r_{a(d)}, x, V_{oc}) = n_{I1(II1)}(V_{ocI1(ocII1)}) + n_{I2(II2)}(V_{ocI2(ocII2)}) \times \left(\frac{V_{oc}}{V_{ocI1(ocII1)}} - 1\right)^{\alpha(\beta)}, \quad (46)$$

where, for example, the values of  $\alpha(\beta)$ , obtained for  $x = (0, 0.5 \text{ and } 1)$ , will be reported in Tables 3n and 5p, for these  $[X(x) \equiv GaAs_{1-x}P_x]$ -alloy junctions.

So, one can determine the general expressions for the fill factors, as:

$$F_{I(II)}(W, N^*, T, r_{d(a)}, x, S; N_{a(d)}, T, r_{a(d)}, x, V_{oc}) = \frac{X_{I(II)}(V_{oc}) - \ln[X_{I(II)}(V_{oc}) + 0.72]}{X_{I(II)}(V_{oc}) + 1}. \quad (47)$$

Finally, the efficiency  $\eta_{I(II)}$  can be defined in the  $n^+(p^+) - p(n)$   $X(x)$  alloy-junction solar cells, by:

$$\eta_{I(II)}(W, N^*, T, r_{d(a)}, x, S; N_{a(d)}, T, r_{a(d)}, x, V_{oc}) \equiv \frac{J_{scI(scII)} \times V_{oc} \times F_{I(II)}}{P_{in.}}, \quad (48)$$

being assumed to be obtained at 1 sun illumination or at AM1.5G spectrum ( $P_{in.} = 0.100 \frac{W}{cm^2}$ ).

It should be noted that the maximal values of  $\eta_{I(II)}$ ,  $\eta_{I\max.(II\max.)}$ , are obtained at the corresponding ones of  $V_{oc} = V_{oc(ocII)}$ , at

which  $\left(\frac{\partial \eta_{I(II)}(W, N^*, T, r_{d(a)}, x, S; N_{a(d)}, r_{a(d)}, x, V_{oc})}{\partial V_{oc}}\right)_{V_{oc}=V_{oc(ocII)}} = 0$ , as those given in next Tables 3n and

5p in Appendix 1, being marked in bold. Further, from the well-known Carnot's theorem, being obtained by the second principle in thermodynamics, or by the entropy law, the maximum efficiency of a heat engine operating between hot (H) and cold (C) reservoirs is the ratio of the temperature difference between the reservoirs,  $T_H - T_C$ ,  $T_C \equiv T = 300$  K, to the H-reservoir temperature,  $T_H$ , expressed as:

$$\eta_{I(II)}(T, V_{oc}) \leq \eta_{I\max.(II\max.)}(T, V_{oc} = V_{oc(ocII)}) \equiv \eta_{Carnot} = \frac{T_H - T_C}{T_H}, \tag{49}$$

for a simplicity, noting that both  $\eta_{I\max.(II\max.)}$  and  $T_H$  depend on  $(W, N^*, T, r_{d(a)}, x, S; N_{a(d)}, r_{a(d)}, x, V_{oc(ocII)})$ -parameters.

**NUMERICAL RESULTS AND CONCLUDING REMARKS**

We will respectively consider the two following cases of  $n^+(p^+) - p(n)$  -junctions such as: HD (As; Sn) X(x) alloy ER – LD (Mg; Cd) X(x) – alloy BR –case, according to: 2 ( $n^+p$ ) – junctions denoted by: (As<sup>+</sup>Mg, Sn<sup>+</sup>Cd), and HD (Mg; Cd) X(x) alloy ER – LD (As; Sn) X(x) – alloy BR –case, according to: 2 ( $p^+n$ ) – junctions denoted by: (Mg<sup>+</sup>As, Cd<sup>+</sup>Sn).

Now, by using the physical conditions, given in Eq. (42), we can determine various photovoltaic conversion coefficients as follows.

**Firs case: HD [ As; Sn ] X(x) – Alloy ER – LD [ Mg; Cd ] X(x) – Alloy BR**

Here, there are the 2 ( $n^+p$ ) – X(x) junctions, being denoted by: (As<sup>+</sup>Mg, Sn<sup>+</sup>Cd).

Then, the numerical results of  $\frac{\tau_{htt}^*}{\tau_{hE}}$ ,  $J_{Bpo}$ ,  $J_{Eno}$  and  $J_{ol}$ , are calculated using Equations (38), (18), (36) and (41), respectively, and obtained, as those given in Table 2n in Appendix 1. Further, those of  $n_I$ ,  $J_{scl}$ ,  $F_I$ ,  $\eta_I$ , and  $T_H$ , are computed, using Equations (46, 45, 47, 48, 49), respectively, and reported in the following Table 3n in Appendix 1.

**Tables 2n and 3n in Appendix 1**

**Second case: HD [ Mg; Cd ] X(x) – Alloy ER – LD [ As, Sn ] X(x) – Alloy BR**

Here, there are 2 ( $p^+n$ ) – X(x)-junctions, being denoted by: (Mg<sup>+</sup>As, Cd<sup>+</sup>Sn).

Then, the numerical results of  $\frac{\tau_{ett}^*}{\tau_{eE}}$ ,  $J_{Bno}$ ,  $J_{Epo}$  and  $J_{oII}$ , are calculated using Equations (38), (18), (36) and (41), respectively, and obtained, as those given in Table 4p in Appendix 1. Further, those of  $n_{II}$ ,  $J_{scII}$ ,  $F_{II}$ ,  $\eta_{II}$ , and  $T_H$ , are computed, using Equations (46, 45, 47, 48, 49), respectively, and reported in the following Table 5p in Appendix 1.

### Tables 4p and 5p in Appendix 1

Finally, some concluding remarks are obtained and discussed as follows.

(1) In Table 3n, for the  $n^+ - p$   $GaP_{1-x}As_x$ -alloy junction solar cell and for  $r_{Sn(Cd)}$ -radius, one obtains with increasing  $x=(0, 0.5, 1)$ :  $\eta_{I\max.}(\sphericalangle)= 32.83 \%$ , 31.96 %, 31.15 %, according to  $T_H(\sphericalangle) = 446.6 \text{ K}, 440.9 \text{ K}, 435.7 \text{ K}$ , at  $V_{ocI} = 1.06 \text{ V}, 1.06 \text{ V}, 1.07 \text{ V}$ , respectively.

(2) In Table 5p, for the  $p^+ - n$   $GaP_{1-x}As_x$ -alloy junction solar cell and for  $r_{Cd(Sn)}$ -radius, one obtains with increasing  $x=(0, 0.5, 1)$ :  $\eta_{II\max.}(\sphericalangle)= 32.51 \%$ , 32.51 %, **33.07 %**, according to  $T_H(\sphericalangle) = 444.5 \text{ K}, 444.5 \text{ K}, 448.2 \text{ K}$ , at  $V_{ocII}(\text{V})[> V_{ocI}(\text{V})] = 1.17 \text{ V}, 1.18 \text{ V}, 1.20 \text{ V}$ , respectively, suggesting that such  $\eta_{I\max.}(\text{I}\max.)$ -and- $T_H$  variations depend on  $V_{ocII}(\text{V})[> V_{ocI}(\text{V})]$  – ones.

(3) Finally, as noted in above remarks (1) and (2), for  $x=1$ , the  $GaP_{1-x}As_x$ -alloy becomes the GaAs-one, and therefore,  $\eta_{I\max.}=31.15 \%$  and  $\eta_{II\max.}=33.07 \%$ , which can be compared with the corresponding results obtained by Moon et al.<sup>[6]</sup> and Green et al.<sup>[4]</sup> for the single-junction GaAs thin-film solar cell, 22.08 % and 29.71 %, respectively, suggesting that in order to obtain the highest efficiencies, the  $GaP_{1-x}As_x$ -alloy junction solar cells could be chosen rather than the crystalline GaAs-junction solar cell.

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APPENDIX 1

**Table 1:** In the  $\text{GaP}_{1-x}\text{As}_x$ -alloy the numerical results of  $B_{\text{do(ao)}}$ ,  $\epsilon$ ,  $E_{\text{gno(gp)}}$ ,  $N_{\text{CDn(CDp)}}$ ,  $E_{\text{gin(gip)}}(r_{\text{d(a)},x}, T)$ , and  $\eta_{\text{n(p)}}(u)$ ,  $u(N^*, T, x) \equiv \frac{N^*}{N_{\text{c(v)}(T,x)}}$ , are computed for physical conditions, given in Eq. (42), using Equations (5), (8a, 8b), (9a), (10), and (12), respectively. Here, on notes that: (i)  $N = 10^{20} \text{cm}^{-3}$  and  $T=300 \text{ K}$ , (ii)  $N^* \equiv N^*(N, r_{\text{d(a)},x}) \equiv N - N_{\text{CDn(NDp)}}(r_{\text{d(a)},x})$ , given in Eq. (9d), and finally (iii) in the limiting conditions: these numerical results are reduced to those given in GaP-crystal for  $x=0$ , and to those given in the GaAs-alloy for  $x=1$ .

Donor		P	As
$r_{\text{d}}$ (nm)	↗	<b><math>r_{\text{do}}=0.110</math></b>	0.118
x	↗	0, 0.5, 1	0, 0.5, 1
$B_{\text{do}}(x)$ in $10^9 \text{ (N/m}^2)$	↘	4.123179, 2.60924, 1.4960608	
$\epsilon(r_{\text{d}}, x)$	↘	<b>11.1</b> , 12.115, <b>13.13</b>	10.83572, 11.82655, 12.817384
$E_{\text{gno}}(r_{\text{d}}, x)$ eV	↗	<b>1.796</b> , 1.658, <b>1.52</b>	1.796708, 1.658448, 1.5202571
$N_{\text{CDn}}(r_{\text{d}}, x)$ in $10^{16} \text{ cm}^{-3}$	↗	16.859958, 5.5552466, 1.3330088	18.123934, 5.9717184, 1.4329432
$E_{\text{gin}}(r_{\text{d}}, x, T)$ in eV		1.72599, 1.57473, 1.42348	1.7267, 1.57518, 1.42374
$\eta_{\text{n}} \gg 1$ (degenerate case)	↘	23.395, 31.027, 46.051	23.393, 31.026, 46.051
Donor		Sb	Sn
$r_{\text{d}}$ (nm)	↗	0.136	0.140
x	↗	0, 0.5, 1	0, 0.5, 1
$\epsilon(r_{\text{d}}, x)$	↘	8.868820, 9.679798, 10.490775	8.3478503, 9.111190, 9.8745293
$E_{\text{gno}}(r_{\text{d}}, x)$ eV	↗	1.8041281, 1.663144, 1.5229492	1.8070212, 1.664974, 1.5239990
$N_{\text{CDn}}(r_{\text{d}}, x)$ in $10^{16} \text{ cm}^{-3}$	↗	33.054297, 10.891176, 2.6133913	39.637063, 13.060155, 3.1338483
$E_{\text{gin}}(r_{\text{d}}, x, T)$ in eV		1.73412, 1.57988, 1.42643	1.73701, 1.58171, 1.42748
$\eta_{\text{n}} \gg 1$ (degenerate case)	↘	23.370, 31.016, 46.047	23.360, 31.012, 46.046
Acceptor		Ga	Mg
$r_{\text{a}}$ (nm)	↗	<b><math>r_{\text{ao}}=0.126</math></b>	0.140
x	↗	0, 0.5, 1	0, 0.5, 1
$B_{\text{ao}}(x)$ in $10^9 \text{ (N/m}^2)$	↘	1.055177, 0.700649, 0.4388991	

$\epsilon(r_a, x) \searrow$	11.1, 12.115, 13.13	10.5002, 11.4604, 12.42055
$E_{gpo}(r_a, x) \text{ eV} \nearrow$	1.796, 1.658, 1.52	1.8024849, 1.66231, 1.5226974
$N_{CDP}(r_a, x) \text{ in } 10^{18} \text{ cm}^{-3} \nearrow$	9.5926026, 3.6514435, 1.142563	11.332043, 4.3135651, 1.3497457
$E_{gip}(r_a, x, T) \text{ in eV} \nearrow$	1.726, 1.5747, 1.4235	1.7325, 1.579, 1.4262
$\eta_p \gg 1$ (degenerate case) $\searrow$	5.9036, 7.6634, 10.4814	5.8328, 7.6298, 10.4671
Acceptor	In	Cd
$r_a$ (nm) $\nearrow$	0.144	0.148
$x \nearrow$	0, 0.5, 1	0, 0.5, 1
$\epsilon(r_a, x) \searrow$	10.143959, 11.0715, 11.999115	9.7367823, 10.62713, 11.51747
$E_{gpo}(r_a, x) \text{ eV} \nearrow$	1.8068933, 1.665233, 1.5245311	1.8125359, 1.66898, 1.5268781
$N_{CDP}(r_a, x) \text{ in } 10^{18} \text{ cm}^{-3} \nearrow$	12.568487, 4.7842197, 1.4970169	14.212125, 5.4098739, 1.6927886
$E_{gip}(r_a, x) \text{ in eV} \nearrow$	1.7369, 1.582, 1.428	1.7425, 1.5857, 1.4304
$\eta_p \gg 1$ (degenerate case) $\searrow$	5.7822, 7.6059, 10.4570	5.7146, 7.5741, 10.4434

**Table 2n:** In the HD [(As; Sn)-GaP<sub>1-x</sub>As<sub>x</sub>-alloy] ER-LD[(Mg; Cd)-GaP<sub>1-x</sub>As<sub>x</sub>-alloy] BR, for physical conditions given in Eq. (42) and for a given x, our numerical results of  $\frac{\tau_{ht}^+}{\tau_{he}}$ ,  $J_{Bpo}$ ,  $J_{Eno}$  and  $J_{oi}$ , are computed, using Equations (38), (18), (36) and (41), respectively, noting that  $J_{oi}$  decreases strongly with increasing  $r_{d(a)}$ -radius for given x, but it increases strongly with increasing x for given  $r_{d(a)}$ -radius, being new results.

$n^+p$	As <sup>+</sup> Mg	Sn <sup>+</sup> Cd
$J_{Bpo} \text{ in } 10^{-24} \text{ (A/cm}^2) \searrow$	3.7256	3.4547
$J_{Eno} \text{ in } 10^{-29} \text{ (A/cm}^2) \searrow$	2.4794	0.1204
$J_{oi} \text{ in } 10^{-24} \text{ (A/cm}^2) \searrow$	3.7256	3.4547

Here,  $x=0$  for the (As<sup>+</sup>Mg, Sn<sup>+</sup>Cd)-junctions, and from Eq. (38), one obtains:  $\frac{\tau_{ht}^+}{\tau_{he}} = (0, 0)$  suggesting a completely transparent condition.

Here,  $x=0.5$  for the  $(As^+Mg, Sn^+Cd)$ -junctions, and from Eq. (38), one obtains:  
 $\frac{\tau_{ht}^+}{\tau_{he}} = (0, 0)$  suggesting a completely transparent condition.

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$J_{Bpo}$ in $10^{-22}$ (A/cm <sup>2</sup> ) $\simeq$	6.9673	6.4608
$J_{Eno}$ in $10^{-26}$ (A/cm <sup>2</sup> ) $\simeq$	1.6784	0.0176
$J_{oi}$ in $10^{-22}$ (A/cm <sup>2</sup> ) $\simeq$	6.9675	6.4608

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Here,  $x=1$  for the  $(As^+Mg, Sn^+Cd)$ -junctions, and from Eq. (38), one obtains:  
 $\frac{\tau_{ht}^+}{\tau_{he}} = (0, 0)$  suggesting a completely transparent condition.

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$J_{Bpo}$ in $10^{-20}$ (A/cm <sup>2</sup> ) $\simeq$	9.4699	8.7814
$J_{Eno}$ in $10^{-22}$ (A/cm <sup>2</sup> ) $\simeq$	8.9188	0.0017
$J_{oi}$ in $10^{-20}$ (A/cm <sup>2</sup> ) $\simeq$	9.5592	8.7814

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**Table 3n:** In the HD [(As; Sn)-GaP<sub>1-x</sub>As<sub>x</sub>-alloy] ER-LD[(Mg; Cd)-GaP<sub>1-x</sub>As<sub>x</sub>-alloy] BR, for physical conditions given in Eq. (42) and for a given x, our numerical results of  $n_I$ ,  $J_{scl}$ ,  $F_I$ ,  $\eta_I$ , and  $T_H$ , are computed, using Equations (46, 45, 47, 48, 49), respectively, noting that both  $\eta_{I_{max}}$  and  $T_H$ , marked in bold, increase with increasing x for given  $r_{d(a)}$ , being new results.

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$V_{oc}(V)$	$n_I$	$J_{scl}(\frac{mA}{cm^2})$	$F_I(\%)$	$\eta_I(\%)$
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Here,  $x=0$ . For the  $(As^+Mg, Sn^+Cd)$  junctions, the value of  $\alpha$  given in Eq. (46) is **1.0805**.

$n^+p$	$As^+Mg; Sn^+Cd$	$As^+Mg; Sn^+Cd$	$As^+Mg; Sn^+Cd$	$As^+Mg; Sn^+Cd$
<b>0.980</b>	0.753; 0.752	27.06; 27.06	90.39; 90.40	23.97; 23.97
1.05	0.803; 0.802	34.60; 34.47	90.43; 90.44	32.72; 32.73
<b>1.06</b>	0.811; 0.809	34.24; 34.25	90.43; 90.44	<b>32.82; 32.83</b>
			<b><math>V_{oc} = 1.06 V</math></b>	<b><math>446.5; 446.6 = T_H(K)</math></b>
1.07	0.818; 0.817	33.86; 33.87	90.42; 90.43	32.76; 32.78
<b>1.1272</b>	0.864; 0.863	29.76; 29.76	90.40; 90.42	30.33; 30.34
2	1.656; 1.653	0.728; 0.724	89.82; 89.83	1.308; 1.301

Here,  $x=0.5$ . For the (As<sup>+</sup>Mg, Sn<sup>+</sup>Cd) junctions, the value of  $\alpha$  given in Eq. (46) is **1.08126**.

$n^+p$	As <sup>+</sup> Mg; Sn <sup>+</sup> Cd	As <sup>+</sup> Mg; Sn <sup>+</sup> Cd	As <sup>+</sup> Mg; Sn <sup>+</sup> Cd	As <sup>+</sup> Mg; Sn <sup>+</sup> Cd
<b>0.980</b>	0.840; 0.839	27.06; 27.06	89.53; 89.55	23.74; 23.75
1.05	0.896; 0.894	33.82; 33.83	89.57; 89.59	31.80; 31.82
<b>1.06</b>	0.904; 0.809	33.64; 34.25	89.57; 89.59	<b>31.94; 31.96</b>
			<b><math>V_{oc1} = 1.06 V</math></b>	<b><math>440.8; 440.9=T_H(K)</math></b>
1.07	0.913; 0.817	33.32; 33.87	89.57; 89.59	31.93; 31.95
<b>1.1272</b>	0.964; 0.863	29.75; 29.76	89.55; 89.56	30.03; 30.04
2	1.847; 1.653	1.064; 0.724	88.92; 88.93	1.893; 1.883

Here,  $x=1$ . For the (As<sup>+</sup>Mg, Sn<sup>+</sup>Cd) junctions, the value of  $\alpha$  given in Eq. (46) is **1.0822**.

$n^+p$	As <sup>+</sup> Mg; Sn <sup>+</sup> Cd	As <sup>+</sup> Mg; Sn <sup>+</sup> Cd	As <sup>+</sup> Mg; Sn <sup>+</sup> Cd	As <sup>+</sup> Mg; Sn <sup>+</sup> Cd
<b>0.980</b>	<b>0.943; 0.941</b>	27.06; 27.06	88.56; 88.58	23.49; 23.49
1.06	1.015; 1.013	33.10; 33.11	88.60; 88.62	31.09; 31.11
<b>1.07</b>	1.025; 1.023	32.84; 32.85	88.60; 88.62	<b>31.13; 31.15</b>
			<b><math>V_{oc1} = 1.07 V</math></b>	<b><math>435.6; 435.7=T_H(K)</math></b>
1.08	1.034; 1.033	32.47; 32.49	88.60; 88.62	31.07; 31.09
<b>1.1272</b>	1.082; 1.080	29.76; 29.77	88.58; 88.60	29.72; 29.73
2	2.073; 2.069	1.522; 1.512	87.89; 87.91	2.675; 2.659

**Table 4p:** In the HD [(Mg; Cd)-GaP<sub>1-x</sub>As<sub>x</sub>-alloy] ER-LD[(As; Sn)-GaP<sub>1-x</sub>As<sub>x</sub>-alloy] BR, for physical conditions given in Eq. (42) and for a given x, our numerical results of  $\frac{\tau_{att}^+}{\tau_{aR}}$ ,  $J_{Bno}$ ,  $J_{Epo}$  and  $J_{oII}$ , are computed, using Equations (38), (18), (36) and (41), respectively, noting that  $J_{oII}$  decreases strongly with increasing  $r_{a(d)}$ -radius for given x, but it increases strongly with increasing x for given  $r_{a(d)}$ -radius, being new results.

$p^+n$	Mg <sup>+</sup> As	Cd <sup>+</sup> Sn
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Here,  $x=0$ , and for the  $(Mg^{+}As,Cd^{+}Sn)$ -junctions and from Eq. (34), one obtains:

$\frac{\tau_{eE}^{+}}{\tau_{eE}} = (0, 0)$  suggesting a completely transparent condition.

$J_{Bno}$ in $10^{-24}$ (A/cm <sup>2</sup> ) $\simeq$	1.6147	0.8348
$J_{Epo}$ in $10^{-27}$ (A/cm <sup>2</sup> ) $\simeq$	1.2926	0.7831
$J_{oII}$ in $10^{-24}$ (A/cm <sup>2</sup> ) $\simeq$	1.6160	0.8356

Here,  $x=0.5$ , and for the  $(Mg^{+}As,Cd^{+}Sn)$ -junctions and from Eq. (34), one obtains:

$\frac{\tau_{eE}^{+}}{\tau_{eE}} = (0, 0)$  suggesting a completely transparent condition.

$J_{Bno}$ in $10^{-22}$ (A/cm <sup>2</sup> ) $\simeq$	2.6082	1.5611
$J_{Epo}$ in $10^{-25}$ (A/cm <sup>2</sup> ) $\simeq$	1.2570	0.7875
$J_{oII}$ in $10^{-22}$ (A/cm <sup>2</sup> ) $\simeq$	2.6095	1.5619

Here,  $x=1$ , and for the  $(Mg^{+}As,Cd^{+}Sn)$  junctions and from Eq. (34), one obtains:

$\frac{\tau_{eE}^{+}}{\tau_{eE}} = (0, 0)$  suggesting a completely transparent condition.

$J_{Bno}$ in $10^{-20}$ (A/cm <sup>2</sup> ) $\simeq$	3.1831	2.1219
$J_{Epo}$ in $10^{-24}$ (A/cm <sup>2</sup> ) $\simeq$	7.7128	4.7505
$J_{oII}$ in $10^{-20}$ (A/cm <sup>2</sup> ) $\simeq$	3.1839	2.1223

**Table 5p:** In the HD [(Mg; Cd)-GaP<sub>1-x</sub>As<sub>x</sub>-alloy] ER-LD[(As; Sn)-GaP<sub>1-x</sub>As<sub>x</sub>-alloy] BR, for physical conditions given in Eq. (42) and for a given x, our numerical results of  $n_{II}$ ,  $J_{scII}$ ,  $F_{II}$ ,  $\eta_{II}$ , and  $T_H$ , are computed, using Equations (46, 45, 47, 48, 49), respectively, noting that both  $\eta_{IImax}$ , and  $T_H$ , marked in bold, increase with increasing x for given  $r_{a(d)}$ , being new results.

$V_{oc}(V)$	$n_{II}$	$J_{scII}(\frac{mA}{cm^2})$	$F_{II}(\%)$	$\eta_{II}(\%)$
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Here,  $x=0$ . For the  $(Mg^{+}As,Cd^{+}Sn)$ -junctions, the value of  $\beta$  given in Eq. (46) is **1.0452**.

$p^{+}n$	$Mg^{+}As;Cd^{+}Sn$	$Mg^{+}As;Cd^{+}Sn$	$Mg^{+}As;Cd^{+}Sn$	$Mg^{+}As;Cd^{+}Sn$
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<b>0.980</b>	0.742; 0.733	24.20; 24.20	90.50; 90.59	21.46; 21.48
<b>1.03</b>	0.777; 0.767	29.90; 29.98	90.53; 90.62	27.88; 27.98
1.16	0.874; 0.863	30.84; 30.92	90.53; 90.63	32.38; 32.51
<b>1.17</b>	0.882; 1.036	30.58; 33.14	90.53; 88.60	<b>32.39; 32.51</b>
			$V_{ocII} = 1.17 \text{ V}$	<b>443.7; 444.5 = <math>T_H</math> (K)</b>
1.18	0.890; 1.083	30.29; 33.14	90.53; 88.60	32.36; 32.47
2	1.553; 3.315	7.035; 33.14	90.31; 88.60	12.71; 12.50

Here,  $x=0.5$ . For the ( $Mg^+As, Cd^+Sn$ )-junctions, the value of  $\beta$  given in Eq. (46) is **1.0476**.

$p^+n$	$Mg^+As; Cd^+Sn$	$Mg^+As; Cd^+Sn$	$Mg^+As; Cd^+Sn$	$Mg^+As; Cd^+Sn$
<b>0.980</b>	0.824; 0.815	24.20; 24.20	89.69; 89.78	21.27; 21.29
<b>1.03</b>	0.863; 0.853	29.74; 29.80	89.72; 89.81	27.48; 27.57
1.17	0.979; 0.968	30.84; 30.92	89.73; 89.82	32.39; 32.49
<b>1.18</b>	0.988; 0.977	30.60; 30.67	89.73; 89.82	<b>32.40; 32.51</b>
			$V_{ocII} = 1.18 \text{ V}$	<b>443.8; 444.5 = <math>T_H</math> (K)</b>
1.19	0.996; 0.985	30.34; 33.40	89.73; 89.82	32.39; 32.49
2	1.724; 1.705	8.022; 7.915	89.49; 89.58	14.36; 14.18

Here,  $x=1$ . For the ( $Mg^+As, Cd^+Sn$ )-junctions, the value of  $\beta$  given in Eq. (46) is **1.0519**.

$p^+n$	$Mg^+As; Cd^+Sn$	$Mg^+As; Cd^+Sn$	$Mg^+As; Cd^+Sn$	$Mg^+As; Cd^+Sn$
<b>0.980</b>	0.921; 0.912	24.20; 24.20	88.77; 88.86	21.05; 21.07
<b>1.03</b>	0.963; 0.953	29.82; 29.88	88.81; 88.90	27.28; 27.36
1.19	1.111; 1.100	31.17; 31.24	88.82; 88.91	32.95; 33.05
<b>1.20</b>	1.121; 1.110	30.93; 30.99	88.82; 88.91	<b>32.97; 33.07</b>
			$V_{ocII} = 1.20 \text{ V}$	<b>447.6; 448.2 = <math>T_H</math> (K)</b>
1.21	1.130; 1.119	30.66; 30.72	88.82; 88.90	32.96; 33.05
2	1.925; 1.906	9.071; 8.974	88.56; 88.65	16.07; 15.91